

Whittle : EXTRAGALACTIC ASTRONOMY

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9. GAS & DUST IN GALAXIES

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(1) Galaxy ISMs : An Overview

- Like the Earth, galaxies have an **atmosphere** → a gaseous component held "down" by gravity this atmosphere fills the space between stars, hence: **interstellar medium** (ISM)
by mass, the ISM is usually not very important: $M_{\text{ISM}} \approx 1\% M_{\text{stars}}$
The **average** midplane density is $\sim 1 \text{ cm}^{-3}$ → columns $\sim 3 \times 10^{21} \text{ cm}^{-2}/\text{kpc}$ ($\sim 0.005 \text{ gm cm}^{-2}/\text{kpc}$)
→ galaxy disks have "thickness" $\equiv 5 \text{ cm}$ of Earth's atmosphere ($\sim 1 \text{ meter}$ of air to the GC).
- The ISM contains: starlight; gas; dust; cosmic rays; magnetic fields
Near the sun they all have similar energy density \equiv pressure $\approx 1 \text{ eV cm}^{-3}$
- The element mix is the usual: H/He/others: 74/24/2 (% by mass); 90/10/0.01 (% by number)
Of the "others", ~ 10 -50% have condensed out as solid particles: "dust".
- Despite its low mass, the ISM is ultimately very important, for several reasons:
 1. It plays a crucial role in the star ↔ gas cycle
 - in spirals and irregulars, it facilitates ongoing (& current) star formation
 - it is a repository for element buildup and is therefore integral to chemical evolution
 2. Because it can cool, its collapse is **dissipational**
 - stars can form !! hot gas → cold gas → stars
 - new generations of stars "cool" spiral disks, allowing arm formation
 - globally, gas can migrate inwards to smaller radii:
→ galaxies are smaller than dark matter halos !

- galaxies have steep density gradients
- galaxy nuclei can have very high densities, including an SMBH

3. Being atomic/molecular, its emission & absorption provides enormous diagnostic information

Some examples :

- Doppler motions reveal galaxy dynamics
- abundance measurements allow study of chemical evolution
- physical conditions: density; temp; pressure; turbulence; columns; mass, can all be derived
- some emission lines can be seen (relatively) easily at cosmological distances.
- high redshift QSO absorption lines reveal halo & disk evolution.

4. The ISM can dominate a galaxy's integrated SED (spectral energy distribution):

starlight dominates the UV-NIR; but the ISM dominates outside this range.

- Mid-IR to Sub-mm is dominated by emission from **dust**
- Soft X-rays come from the **hot ISM phase** (though X ray binaries can be important)
- cm-radio comes either from **HII regions** or a **relativistic magnetoionic plasma**
- certain emission lines (eg Ly α ; [CII] λ 158 μ) can be **major coolants**

• The ISM is energized primarily by **stars** (starlight, winds, supernovae)

- UV starlight photoionizes atoms & dissociates molecules; photo-ejected electrons heat gas
- SN shocks heat/ionize/accelerate gas & are largely responsible for the ISM's complexity.

• The ISM can be highly **inhomogeneous**, with several **phases**

These phases are (roughly): hot/warm/cold, with low/medium/high density

In a wide range of conditions these phases have **similar pressures** → $P/k \equiv nT \approx 10^4 \approx 1 \text{ eV cm}^{-3}$.
However, in dynamic situations, pressure balance is no longer applicable.

The ISM contains **cloud** and **intercloud** components with density contrast $\sim 10^2$ - 10^5

→ these clouds are not like terrestrial clouds; more like blocks of wood or lead hanging in the air.

• The ISM is a **dynamic environment**, with **mass exchange** between phases

- cooling facilitates: hot → warm → cold → stars.
- supernovae inject energy which accelerates the gas and continuously rearranges the geometry
→ e.g. a disk ISM will "boil" & "bubble" with gas cycling out & back above the disk.
- sporadically, tidal encounters & their resulting starbursts can:
 - add fresh (low metallicity) gas
 - energize and evacuate large regions
 - cycle gas into the halo, some of which may return later.
 - radically alter the ISM, e.g. spiral + spiral → elliptical.

As always, our current view is just one frame of a long and intricate movie.

• What about the **distribution** of ISM (particularly in spiral disks)?

1. **Globally** the scale height depends on the phase's temperature/velocity dispersion and $\nabla\phi$

- colder phases are confined closer to the plane
 - hotter &/or more turbulent phases are thicker
 - in disks, the ISM flares at large radii and is thinner at small radii).
- However, high local energy density can affect this distribution by driving vertical blow-out.

2. **Locally**: the ISM is highly complex & "foamy"

SN evacuate complex interconnected "superbubbles"
between are sheets & clouds of denser colder gas.

• The Milky Way can act as a **template** for studying other galaxy ISMs

As usual, the proximity of the MW's ISM offers important insights

Hence, MW ISM studies are now extensive & comprise a major area within astronomy

Here, we consider only the bare essentials, providing a framework for discussing ISM in other galaxies.



(2) ISM Components & Their Observational Signatures

(a) Introduction

While ultimately ISM gas spans all conditions, in practice much resides in one of several **components**. These components are distinguished by their **phase** (n, T, X_e) and their **location**.

This [figure](#) and the following table summarize the major components:

Component	Temp K	Density midplane cm^{-3}	Pressure nT K cm^{-3}	X_e ionization	FF filling %	$\langle h \rangle$ thickness pc
Intercloud						
Hot HII (HIM)	10^6	0.002	2000	1	50:	3000:
Warm HII (WIM)	8000	0.15	1200	1	20	1000
Warm HI (WNM)	8000	0.3:	2400	0.5	30:	500
Clouds						
Cold HI (CNM)	120	25	3000	0.1	2	100
Cold H ₂ (CNM)	15	200	3000	10^{-4}	0.1	75

Note that overall, the intercloud/cloud fraction by mass is $\sim 50 : 50$ but by volume it is $\sim 98 : 2$

- Three other important components add to the mix :
 1. **Dust:** 1nm - $1\mu\text{m}$ solid particles are found in essentially all phases
 $\sim 50\%$ heavy elements are in dust ($\sim 100\%$ of the refractories)
 Dust is discussed more in section 8 ([link](#))
 2. **Magnetic fields:** generally a few μGauss in both ordered and random components
 energy density: $B^2/8\pi \approx 10^{-12} \text{ erg cm}^{-3} \approx 1 \text{ eV cm}^{-3}$
 field compression in superbubble expansion effects on ISM structure (see below).
 3. **Cosmic Rays:** relativistic electrons & protons, created in SN shocks
 these diffuse throughout the galaxy and permeate all phases (some even hit the earth)
 they are a primary heating source in DMC cores (which are otherwise shielded).
 the most energetic electrons + magnetic fields \rightarrow radio synchrotron
 proton collisions with nuclei \rightarrow diffuse gamma emission
 equipartition with B field likely, so suspect $\sim 1 \text{ eV cm}^{-3}$

(b) Observational Signatures: General Considerations

All observations involve either emission or absorption
 these, in turn, depend on **Emission Measure** (EM) and **column density** (N)

- Emission processes are usually **collisional**, so are $\propto n^2$

surface brightness is therefore $\propto \int \langle n^2 \rangle dl \text{ pc cm}^{-6} \equiv \text{Emission Measure (EM)}$.

- Absorption processes, in contrast, are $\propto \int \langle n \rangle dl \text{ cm}^{-2} \equiv \text{Column Density (N)}$.
- For ionized gas, the relevant density is usually n_e
The table shows EM & N_e for various systems:

Medium	n_e cm^{-3}	Size pc	EM pc cm^{-6}	Emission Visibility	N_e cm^{-2}	Absorption Visibility
Young Nova	10^7	10^{-3}	10^{11}	v. bright!	3×10^{22}	thick
PN	10^4	10^{-1}	10^7	bright	3×10^{21}	good
HII Region	10	10^2	10^4	fine	3×10^{21}	good
Diffuse ISM	10^{-1}	10^3	10	difficult	3×10^{20}	good
Halo	10^{-3}	10^4	10^{-2}	invisible	3×10^{19}	fine

Note, for a typical crosssection $\sim a_{\text{Bohr}} \sim 10^{-16} \text{ cm}^{-2}$, $N \sim 10^{14} \text{ cm}^{-2}$ gives $\tau \sim 1\%$
This is easily measurable with suitable background source
→ low density gas invisible in emission can often be studied in absorption.

- Photoionization thresholds render the ISM highly opaque in the EUV:
ionization potentials X for H, He, He⁺ are 13.6, 24.6, 54.4 eV (= 91, 50, 25 nm)
since $\sigma_{\text{photo}} \propto (E - E_i)^{-3}$, then:
 - the ISM is **highly opaque** in EUV (13.6 - 100 eV)
 - it is becoming transparent in soft X-ray (~0.6 keV)
 - it is completely transparent by 2 keV.
- A wide range of δE transitions yield features at many wavelengths:

Transition δE eV	wavelength range	Cause
10^{-6}	21 cm	electron spin flip in atomic H
$10^{-2} - 10^{-3}$	FIR - mm	molecular rotation
0.1 - 0.01	NIR - FIR	gas molecular vibration; bond bending in dust
0.03 - 0.003	MIR - sub-mm	phonons in dust @ $T \sim 1000\text{-}10 \text{ K}$
1 - 10	UV - NIR	outer shell electron transitions in atoms <u>and</u> molecules
$10 - 10^3$	EUV - X-ray	inner shell electron transition; $50 - 500 \text{ km s}^{-1}$ post shock gas

Note some useful conversions: $E_{\text{eV}} \equiv 1240/\lambda_{\text{nm}} \equiv T_{\text{K}} / 7740$ per particle.

so @ $T \gtrsim 10^5 \text{K}$, H & He are fully ionized, and $kT \sim \text{EUV} - \text{soft X-ray}$

(c) Warm Ionized Gas

- This gas has $T \sim 8000\text{K}$ and resides in:
 - star forming HII regions ($n_e \sim 1 - 100+ \text{cm}^{-3}$)
 - diffuse ionized gas ($n_e \sim 0.01 - 1 \text{cm}^{-3}$)
 - In both cases, equilibrium occurs when:
 - ionization rate = recombination rate (ionization balance)
 - heating = cooling (thermal balance)
- ionization** is from stellar UV photons; **recombination** occurs naturally
heating is from photo-ejected electrons; **cooling** is via emission lines
- Note that in these circumstances the ionization degree **does not** reflect the temperature
 e.g. at 8000K, $\text{O} \rightarrow \text{O}^+ \rightarrow \text{O}^{2+}$ cannot occur by collisions (it is too cold)
 but a weak radiation field of 50 eV (250A) photons can ionize up to O^{2+} .

(i) Hydrogen Recombination Radiation

- electrons are captured by protons and the resulting cascade emits photons.
 the rate is $\alpha n_e n_p \text{cm}^{-3} \text{s}^{-1}$, where α is a recombination coefficient (units are $\text{cm}^3 \text{s}^{-1}$).
- Usually, the gas is optically thick to Ly- α , which is trapped (termed: case B)
 the **total** recombination rate is then $\alpha_B = 4.52 \ \& \ 2.58 \times 10^{-13} \text{cm}^3 \text{s}^{-1}$ (for 5000 & 10,000 K)
 While for just H β it is $\alpha_{H\beta} = 5.38 \ \& \ 3.01 \times 10^{-14} \text{cm}^3 \text{s}^{-1}$ (for 5000 & 10,000 K)
- The table gives some useful Hydrogen line wavelengths and relative strengths (Case B; $T = 10^4 \text{K}$):

Series (lower level)	α wav ratio/H β	β wav ratio/H β	γ wav ratio/H β	δ wav ratio/H β	Series Limit wav
1: Lyman	1216 A_{vac} 23	1026 A_{vac} ??	973 A_{vac} ??	950 A_{vac} ??	912 A_{vac}
2: Balmer	6563 A 2.86	4861 A 1.00	4340 A 0.47	4101 A 0.26	3646 A
3: Paschen	1.87 μ 0.339	1.28 μ 0.163	1.09 μ 0.090	1.00 μ 0.055	0.82 μ
4: Brackett	4.05 μ 0.080	2.63 μ 0.045	2.16 μ 0.028	1.94 μ 0.018	1.45 μ

Note that the Ly- α flux is often difficult to predict:
 it is resonantly scattered and either:

it is absorbed by dust, or
 the $2 \rightarrow 1$ transition goes via 2-photon decay

- Cascades between very high n (~ 100) give **radio recombination lines**
 e.g. H109 α at 5.8cm comes from transitions $n=109 \rightarrow 108$

These lines are useful since they are unaffected by dust; though they are quite weak.

(ii) Collisionally Excited Fine Structure Lines

•

(d) Hot Ionized Gas

(e) Warm & Cold Atomic Gas

(f) Molecular Gas

(g) Dust

(h) Relativistic Component

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(3) Theories of the Multi-Phase ISM

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(4) Gas in Disk Galaxies

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(8) Dust: Particles in the ISM

(a) Overview

- All ISM **gas** phases are optically **transparent** (or very nearly)
However, the Milky Way shows patchy **obscuration** of background starlight ([image](#))
What causes this optical absorption? → **solid particles** with size $\approx \lambda_{\text{light}}$ (nm - μm)

Astronomers call these particles "**dust**", though a better word might be "smoke".

- By human standards, the ISM is **exceedingly filthy**.
Imagine bringing the ISM to atmospheric number density ($3 \times 10^{19} \text{ cm}^{-3}$)
→ it would be a **thick smog** with ~ 1 mag/meter [~ 1 mag/inch at ρ_{air}] !!
→ You could not see across a room [your hand in front of your face] !!
→ Walking just a few paces, you'd be covered in an extremely fine black soot.
→ This is a chain-smoker's heaven/nightmare: the smoke is rich in carcinogenic PAHs.
- Why is the ISM so dirty ? Because stars are **dirty furnaces**.
For 10 Gyr they've been "polluting" the ISM by making & blowing off **heavy elements**
Typically, 10-50% of these elements condense as tiny solid particles: graphite/silicates/ices
→ Our atmosphere is clear by comparison because it doesn't contain $\sim 1\%$ particulates.
- Dust has a huge impact on EM radiation, spanning **3 decades** ($\sim 1000\text{\AA} - 100\mu\text{m}$).
It **absorbs** UV & optical but is transparent in the IR (grains have size $\sim \lambda_{\text{UV}}$).
→ important contributions have come from Copernicus, IUE, HST.
It **emits** in the IR (since its equilibrium temperature is $\sim 10\text{-}100\text{K}$)
→ important contributions have come from IRAS, COBE, ISO, Spitzer.

(b) Quick estimates of some important dust properties

Let's gain some insights from a simplified, yet useful, treatment.

Assume an ISM metallicity of $Z \sim 2\%$ (by mass) of which $f_d \sim 0.1$ is condensed as grains.

Assume all grains have dimension a ($\sim 0.1\mu\text{m}$) and density ρ ($\sim 1 \text{ gm cm}^{-3}$).

The grains absorb and emit as black bodies modified by efficiencies $Q_{\text{abs}}(\lambda)$ and $Q_{\text{em}}(\lambda)$

In reality, $Q_{\text{abs}} \sim 1$ in the UV, and $Q_{\text{em}} \ll 1$ in the IR (see below)

However, for now let's take $Q_{\text{abs}} = Q_{\text{em}} = 1$ (perfect black bodies)

(i) H column for significant dust opacity

What hydrogen column has geometrical covering factor 1 in dust particles?

- In terms of the hydrogen column, $N_{\text{H}} \text{ cm}^{-2}$, the projected mass density in dust is simply:
 $N_d \rho a^3 = N_{\text{H}} m_p Z f_d \text{ gm cm}^{-2}$ where $N_d \text{ cm}^{-2}$ is the column in dust.

Substituting for N_d , the total **geometrical cross section** in dust particles is :

$$N_d a^2 = (N_{\text{H}} m_p Z f_d) / (\rho a^3) \times a^2 \approx 3 \times 10^{-22} \times N_{\text{H}} f_d (Z/Z_{\odot}) \times (\rho a_{\mu})^{-1} \text{ cm}^{-2}$$

where ρ is in gm cm^{-3} , a is in μm , and $Z_{\odot} = 0.02$ is solar metallicity.

(using a^2 is OK here, since the absorption efficiency $Q_{\text{abs}} \sim 1$ in the UV/opt).

- For our fiducials, unit covering factor ($N_d a^2 \sim 1 \text{ cm}^{-2}$) occurs for $N_{\text{H}} \sim 3 \times 10^{21} \text{ cm}^{-2}$
Thus, hydrogen columns $\sim 10^{21.5} \text{ cm}^{-2}$ mark when dust absorption will be important.
In fact, this simple estimate is very close to the observed value: $A_V \approx N_{\text{H}} / (2 \times 10^{21})$ mags.
- Using the observed value, paths through the ISM suffer an absorption $A_V \sim 1.6 \times n_{\text{H}} d_{\text{kpc}}$ mags
→ Spiral disks are optically thick **in the plane**, for which $\langle n_{\text{H}} \rangle \sim 1 \text{ cm}^{-3}$
→ However, with $N_{\text{H}} \sim 10^{21} \text{ cm}^{-2}$ **perpendicular** to spiral disks, they are borderline transparent.
→ DMCs are extremely opaque, since $n_{\text{H}} \sim 10^5$ gives $A_V \sim 100$ mag across 1 pc.
→ The hot phase ($n_{\text{H}} \sim 10^{-3} \text{ cm}^{-3}$) is transparent (even without likely dust destruction).

(ii) Dust number density

Continuing briefly, the dust particle number density is:

- $n_d/n_H = (m_p Z f_d) / (\rho a^3) = 3.3 \times 10^{-14} (Z/Z_\odot f_d) / (\rho a_\mu^3) = 3.3 \times 10^{-12}$ for $a \sim 0.1 \mu\text{m}$ and $f_d \sim 0.1$
For $n_H \sim 1 \text{ cm}^{-3}$ (the ISM average) this gives $n_d \sim 1 \text{ per } (100\text{m})^3$;
For $n_H \sim 10^6 \text{ cm}^{-3}$ (a DMC core) it is $\sim 1 \text{ m}^{-3}$
→ dust particles are **few and far between** !!

(iii) Dust Temperature

- In the ISM, ambient starlight usually has a much greater energy flux than local particles.
→ dust is heated mainly by starlight
At equilibrium, therefore, starlight heating balances radiative cooling
There are two common geometries:
 1. For **isotropic** starlight flux $J_s \text{ erg/s/cm}^2/\text{sr}$ we have:
$$4\pi J_s \pi a^2 Q_{\text{abs}} \approx 4\pi a^2 \sigma T_d^4 Q_{\text{em}} \rightarrow T_d \approx (\pi J_s / \sigma)^{1/4} (Q_{\text{abs}}/Q_{\text{em}})^{1/4}$$
 2. For a distance d from a **point source** of luminosity L_\star we have:
$$L_\star / (4\pi d^2) \pi a^2 Q_{\text{abs}} \approx 4\pi a^2 \sigma T_d^4 Q_{\text{em}} \rightarrow T_d \approx (L_\star / 16\pi d^2 \sigma)^{1/4} (Q_{\text{abs}}/Q_{\text{em}})^{1/4}$$

Both are independent of a , and T_d applies equally for interstellar asteroids, planets, or people.
[This is not quite true, since both Q s do in fact depend on a].

- Consider dust in the general interstellar radiation field. What is J_s ?
It is roughly what we witness on a clear moonless night, $\sim 0.002 \text{ erg/s/cm}^2/\text{sr}$.
For $Q_{\text{abs}} = Q_{\text{em}} = 1 \rightarrow T_d \approx 3.2\text{K} \rightarrow$ interstellar space feels very cold!
This result was first obtained by Eddington in 1926.
- This value is, in fact, too low by about $\times 5$.
The reason is that dust **does not behave like a black body**
It absorbs UV better than it radiates IR → a **"green-house" effect**.
The correction factor, $[Q_{\text{abs}}(\text{UV})/Q_{\text{em}}(\text{IR})]^{1/4}$ is discussed below (link).
- Dust embedded in HII regions is exposed to a more intense radiation field.
From 2 we have: $T_d \approx 0.62 \times [(L_\star/L_\odot) / d_{\text{pc}}^2]^{1/4} (Q_{\text{abs}}/Q_{\text{em}})^{1/4} \text{ K}$
giving $T_d \sim 10\text{K}$ for $L_\star \sim 10^5 L_\odot$ and $d \sim 1\text{pc}$ (with $Q_{\text{abs}} = Q_{\text{em}} = 1$)

Again, this is a factor of a few too low, but still illustrates just how cold dust usually is.

- Dust never achieves high enough temperature to emit outside the IR because:
 - it has no internal energy source
 - it's only energy input is starlight
 - it can emit with fairly high efficiency, because it is a solid
 - it behaves as a macroscopic, not quantum, system (with one exception, see below)
 - above $\sim 1500\text{K}$ it evaporates → it **never** contributes below the Near-IR

(iv) Dust Emission Efficiency

- In a typical spiral, $M_{\text{ISM}} \approx 0.05 M_{\text{stars}}$ and $M_{\text{dust}} \approx 0.01 M_{\text{ISM}}$ giving $M_{\text{dust}} \approx 0.0005 M_{\text{stars}}$
However, within factors of a few, $L_{\text{IR}} \approx L_{\text{opt}}$ and we discover that $L_{\text{dust}} \approx L_{\text{stars}}$
How can such a tiny mass of very cold dust compete with nuclear furnaces $10^4 \times$ more massive?
→ dust has a huge **surface area to mass ratio**
- Consider the sun: it has $1 M_\odot$, and a surface with area $A_\odot = 1.3 \times 10^{11} \text{ cm}^2$, at $T_\odot \sim 6000\text{K}$

Now consider $1 M_{\odot}$ of ISM with 2% heavy elements in dust with $a \sim 0.1 \mu\text{m}$ and $\rho \sim 1 \text{ gm cm}^{-3}$
 That makes 4×10^{46} grains with total surface area $5 \times 10^{37} \text{ cm}^2 \sim 10^{15} A_{\odot}$!!
 Per unit area, the dust has vastly lower radiative efficiency:

$$(T_d/T_{\odot})^4 \sim (10/6000)^4 \sim 10^{-11}$$

$$Q_{\text{em}}(\text{IR}) \sim 10^{-4} \text{ relative to black body efficiency (see below)}$$

After integrating over populations of both dust and stars:

→ dust is a more efficient radiator than stars, per unit mass

(c) The Importance of Dust

For our purposes, dust is important for least two reasons

1. it can significantly affect our view of galaxies :
 - it blocks UV and optical, which may need correcting
 - its emission may enhance or even dominate a galaxy's IR emission
2. it can significantly affect crucial ISM processes:
 - it facilitates ISM chemistry (surface catalysis)
 - it can alter HII region structure (e.g. via Ly α destruction)
 - it dominates DMC cooling, helping star formation
 - it can effectively short circuit the deposition of UV/optical input to the ISM (absorbing and then reradiating in the FIR; e.g. starbursts & AGN).

(d) The Path Ahead

- The simple estimates in (b) above hide a multitude of details
 Specifically, we want to explore:
 - the composition of grains and their size distribution
 - the life cycle of grains: origin, growth and destruction
 - dust's affect on light: its emission and absorption properties
 - whether dust properties depend on environment (e.g. different ISM phases)
 - dust's contribution to galaxy SEDs (spectral energy distributions)



(9) Dust: Physical Properties

Ascertaining the properties of dust grains has been remarkably difficult, and is still incomplete.

There are two main reasons for this difficulty:

- They are solids; most astrophysical material is ionic/atomic, with simpler associated physics
- Because they are solids, they have more complex/unclear spectral signatures

Nevertheless, progress has been steady, and the subject is now quite sophisticated.

Here we cover just the basic results.

(a) Dust Composition From ISM Gas Depletion

- If heavy elements reside in dust, they must be missing from the ISM gas.
 One can study dust composition by studying **gas depletion**
 Gas phase abundances are measured from interstellar absorption lines in stellar spectra.

- **The depletion index** is defined logarithmically:

$$D(X) = \log_{10}[N(X)/N(H)]_{\text{obs}} - \log_{10}[N(X)/N(H)]_{\text{ISM}}$$

where $[N(X)/N(H)]_{\text{ISM}}$ is the normal relative abundance of element X (usually taken to be solar).

For example, $D(C) = -0.7$ means C/H is only 20% of its expected value \rightarrow 80% must be in dust.

- Measurements of diffuse clouds ($n_H \sim 10\text{-}100 \text{ cm}^{-3}$) shows **significant total depletion** $\sim 50\%$.
Expressed as a total "metallicity", $Z_d \sim 0.008$ (where $Z_{\odot} = 0.016$)
 \rightarrow $\sim 1\%$ of the ISM is in dust, or equivalently $\sim 50\%$ of ISM metals reside in dust.
- However, the depletion varies greatly from element to element.
Specifically, depletions increase with **condensation temperature**, T_c (see figure).
[$T_c(X)$ is the temperature when 50% of element X is solid, for equilibrium conditions]
e.g. Al, Ca, Ti, Fe, Ni are $\sim 100\%$ depleted, while C, N, O, S, Zn show modest or no depletion.
 \rightarrow dust formation involves condensation/adsorption, & not all elements bind efficiently to dust.
- Depletions also vary with **environment**: (see figures)
depletion is less for hotter/turbulent ISM & higher velocity clouds
 \rightarrow harsh environments (eg shocks) destroy dust &/or prevent it growing
depletion increases with ISM gas density, at least for some elements
 \rightarrow higher densities facilitate grain growth via adsorption
- In terms of total mass, depletions give the following **overall content for dust**:
O: 50% C: 20% Fe: 13% Si: 7% Mg: 6% others: 5%
How they are combined is less clear, though IR spectral features help:
 \rightarrow Silicon is in silicates ($X\text{SiO}_3$ pyroxines; $X\text{SiO}_4$ olivines), where X is mainly Mg, with some Fe.
 \rightarrow Carbon is in graphite, Polycyclic Aromatic Hydrocarbons (PAH), and amorphous carbon
 \rightarrow Fe in metallic iron inclusions
(these results do not include the various ices which probably condense onto dust in DMCs)
- The depletion patterns support a dust model with **resilient refractory core + transient mantle**
The elements Fe, Ti, Ni, Ca are primarily core while Mg and Si can be gained and lost.
- Here's a table which summarizes the various dust populations and their properties: [figure](#)

(b) Dust Creation

- There are several sites of dust formation ([images](#))
 1. winds from evolved RG and AGB stars
 2. winds from young massive stars (e.g. η Carina).
 3. nova ejecta
 4. supernova ejecta
 5. directly from gas phase condensation
- These all involve outflowing winds with decreasing density and temperature
Refractory seeds form and grow by adsorption
The growth rate depends on the wind density, temperature, velocity, and time in the flow.
The growth is non-equilibrium -- simple condensation tracks won't work
The growth also involves feedback:
As dust forms \rightarrow radiation pressure increases \rightarrow wind speed increases \rightarrow stops dust growth.
- There are **two types of winds** ([figures](#))
 1. O-rich winds \rightarrow make silicate grains
metal oxide seeds (e.g. Al_2O_3 ; CaTiO_3)
silicate mantles added (e.g. MgSiO_4 forsterite; MgSiO_4 enstatite)
Fe may also be included (e.g. FeSiO_3 pyroxene).
 2. C-rich winds \rightarrow make graphite & Polycyclic Aromatic Hydrocarbon (PAH) grains
 C_2H_2 (acetylene) nucleation \rightarrow 1-few benzene rings \rightarrow PAHs
grow to $\sim 10\text{-}50\text{ \AA}$ (~ 500 atoms), so these are **small** grains.

(c) Subsequent Growth and Destruction of Grains

- In some environments, **grains can grow** by adsorption most efficient when $kT_{\text{gas}} \approx \epsilon_{\text{phonon}}$ so collisions lose energy to lattice and adhere → results in depletion of metals from the gas phase
Examples:
 - in cold DMCs, grains can grow ice mantles (e.g. H₂, CO, CO₂, CH₄)
 - in proto-stellar disks it is sufficiently dense for grain + grain coagulation → large "fluffy" grains ($\gtrsim 1 \mu\text{m} \lesssim 75\%$ filling factor).
- Many environments are **hostile to grains**
 - Near stars, photon heating can sublimate icy mantles
 - More extreme radiation environments can sublimate the entire grain (e.g. near AGNs, $T_{\text{dust}} \gtrsim 1000\text{K}$).
 - Shocks from SNRs and stellar winds → high kT particles → "sputtering"
 - $> 400 \text{ km s}^{-1}$ → ion-grain sputtering
 - $< 400 \text{ km s}^{-1}$ → grain-grain shattering
 both tend to break up grains → power law size distribution (see below). ultimately, shocks and high T ISM phases can destroy grains completely.

(d) Dust Grain Size Distribution

- **Grain sizes span three decades:** $0.001 \mu\text{m}$ (1nm) → $1 \mu\text{m}$ ($\sim 100 \rightarrow 10^{11}$ atoms)
That's equivalent to salt grains → basket balls!
Clearly, within this huge range one might expect quite distinct grain populations, perhaps with different compositions, origins and histories ([images](#)).
- The final grain size distribution depends on :
 - the injected size distribution from stellar winds
 - subsequent modification by growth and destruction processes.
 Both these can vary from location to location
- The final mix usually contains varying amounts of the following components:
 1. **A "classical" population** of relatively large, dielectric (silicate?) grains
There is evidence for a power law size distribution: $dn/da \propto a^{-3.5}$ with $a_{\text{max}} \sim 0.3 \mu\text{m}$
This population explains:
 - the basic λ^{-1} form of the UV/optical extinction curve;
 - large scattering efficiency ($\sim 60\%$) and scattering angle ($\sim 45^\circ$) in the optical
 - a_{max} comes from dust's IR transparency
 2. **Very small grains** (nano-grains) are required in several contexts:
 - almost isotropic scattering in the FUV
 - the 2175Å broad near-UV absorption feature suggests $\sim 20 \text{ nm}$ graphite grains
 - 2-20 μ emission → $T_d \sim 1000\text{K}$ → single photon heating of $\lesssim 100$ atom grains (see below)
 3. **Large grains** $\sim 1\text{-}10 \mu\text{m}$ can form in **DMC cores**
Only in these sheltered environments can ices condense and grains coagulate
these grains are found in **solar system materials** (a relic of formation)
they are very cold, and should emit in the extreme FIR and sub-mm (invisible to IRAS).
other evidence & statements ? (TBD)
- Different extinction laws can be explained by different proportions of these components [[10biv](#)]

(e) Interaction with Light: Mie Theory

If you assume grains are spheres with uniform refractive index, they yield to classical electrodynamics.

This was first worked out by G. Mie in 1908 (in a different context), and the theory goes by his name. Being a classical theory, wavelength and grain size enter only as their ratio: $X = 2\pi a/\lambda$. Here, we only note a few important results.

- First, recall a **general refractive index is complex**, $m = n - ik$, where k tracks absorption. Ices are good dielectrics, so k is small and n is roughly independent of wavelength. Metals have $k \sim n$ and both may vary significantly with wavelength.
- Absorption and scattering **efficiencies**, Q_{abs} Q_{sca} , are expressed **relative to geometrical** :
e.g. for a particular grain/wavelength/index, Mie theory evaluates (see figure, for $m = 1.5 - 0.05i$)

$$Q_{\text{abs}}(X,m) = (\text{absorption cross-section}) / \pi a^2$$

$$Q_{\text{sca}}(X,m) = (\text{scattering cross-section}) / \pi a^2$$
 which define
 extinction efficiency : $Q_{\text{ext}} = Q_{\text{abs}} + Q_{\text{sca}}$
 and albedo : $\text{Alb} = Q_{\text{sca}} / Q_{\text{ext}}$
- Scattering can be studied by observing reflection nebulae and the diffuse galactic light. In the optical and UV, **scattering is significant** with $\text{Alb} \sim 0.6$ (figure)
 → grains have significant dielectric character, consistent with silicates.
- The mean scattering **angle** can reveal grain **size**:
forward for $\lambda \ll a$ → isotropic for $\lambda \gg a$
 Observations suggest :
 → significant ($\sim 45^\circ$) angle in optical, **increasing** (more isotropic) in UV
 → optical scattering grains have $a \sim 0.1-0.3 \mu\text{m}$,
 → UV scattering grains are much smaller
- In the limit of $\lambda \ll a$, Mie theory gives: (figures)
 $Q_{\text{abs}} = 1$ (ie πa^2 as expected, independent of wavelength)
 $Q_{\text{sca}} = 1$ (also πa^2 , from diffraction)
 $Q_{\text{ext}} = Q_{\text{abs}} + Q_{\text{sca}} = 2$, which is double the simple geometrical cross section.
- In the limit of $\lambda \gg a$ (i.e. $X = 2\pi a/\lambda \ll 1$), Mie theory gives:
 $Q_{\text{abs}} \approx -4 X \text{Im}[M] \propto \lambda^{-1} \text{Im}[M]$ where $M = (m^2 - 1)/(m^2 + 2)$
 $Q_{\text{sca}} \approx 8/3 X^4 |M|^2 \propto \lambda^{-4}$
 → For pure dielectrics (m real, $k = 0$) then $Q_{\text{sca}} = Q_{\text{ext}} \propto \lambda^{-4}$ and we recover Rayleigh scattering.
 → For some absorption (m complex, $k \neq 0$) then $Q_{\text{ext}} \approx Q_{\text{abs}} \propto \lambda^{-1}$
 which is the correct form for the extinction law in the near, mid and far-IR
 → confirming that there are no very large grains ($a \ll 1$ - few μm).
- Mie theory calculates $Q_{\text{abs}}(\lambda)$ for absorption, but what about **emission**: $Q_{\text{em}}(\lambda)$?
 By great good fortune, they are the same !!
 → Recall Kirchoff's law: "good (bad) absorbers are good (bad) emitters".
 more specifically, for thermal emission:
 $F_{\text{em}}(\lambda) = Q_{\text{em}}(\lambda) \times B_\lambda(T)$ per unit area, where $B_\lambda(T)$ is the Planck function; and
 $Q_{\text{em}}(\lambda) = Q_{\text{abs}}(\lambda)$ whose functional form is given above
 (this has its roots in the reversibility of all interactions; a principle called "detailed balance")
- It is now clear that since dust grains **don't** absorb much in the IR, they will be **poor IR emitters**
 Of course, being good emitters in the UV doesn't help, since $B_{\text{UV}}(T)$ is tiny when $T \sim \text{few K}$!
 We now have the "green-house" factor:

$$\rightarrow Q_{\text{abs}}(\text{UV}) / Q_{\text{em}}(\text{IR}) \equiv Q_{\text{abs}}(\text{UV}) / Q_{\text{abs}}(\text{IR})$$

(f) Dust Temperatures

(i) Inferred from IR emission

- First, recall the basic Wein relations for the peak of the Planck function (there are two of them!)
 - The peak of $B_{\lambda} d\lambda$ is at $\lambda \approx 2900\mu\text{m}/T(\text{K})$
 - The peak of $B_{\nu} d\nu$ is $\nu \approx 2.82kT/h$ or $\lambda \approx 5000\mu\text{m}/T(\text{K})$
 - \rightarrow Often, the difference won't matter.
 - \rightarrow Sometimes it does: so check if spectra are in f_{λ} vs λ or f_{ν} vs ν (e.g. Jy vs λ^{-1}).
- In fact, since dust's radiative efficiency $Q_{\text{em}} \propto a/\lambda$ (see below)
 - \rightarrow even a single T_d & single size population doesn't yield a Planck function!
 - In reality, a range of T_d and grain sizes undermines a straightforward inference of T_d
 - Nevertheless, emission in NIR (1-5 μm) MIR (5-25 μm) and FIR (25-300 μm) sub-mm (300-1000 μm) does indicate clearly different mean values of T_d .
- Overall, dust emission can span a broad range, NIR to FIR (sub-mm at higher redshift):
 - $\rightarrow T_d$ spans a wide range: 1000 - 10K, however ...
 - In most galaxies, the bulk is in the FIR, $\sim 60 - 200\mu\text{m}$
 - \rightarrow the majority of dust has $T_d \sim 10 - 50\text{K}$

(ii) Equilibrium T_d Estimates

- The zeroth order calculation was done in 8-b-iv above: (link)
 - \rightarrow dust heating balances black body cooling, with both modified by efficiency (Q) factors
 - For pure black bodies, this yields the Eddington values, which are **too low** by factors \sim few.
- To improve on this we need :
 - the absorption and emission efficiencies, $Q_{\text{abs}}(a, \lambda, m)$ and $Q_{\text{em}}(a, \lambda, m)$
 - which need integrating over grain size distribution, and incident and outgoing spectra
 - if the region is ionized, one should include the important isotropic trapped Ly α field
 - any collisional heating terms should also be included
- Let's consider the most important factors: Q_{abs} and Q_{em}
 - Treating grains as black bodies: $Q_{\text{abs}} = Q_{\text{em}} = 1$ at all λ is:
 - OK in the UV - they are good absorbers
 - BAD in the IR - they are poor emitters (since $a \ll \lambda$).
 - \rightarrow the correction factor $[Q_{\text{abs}}(\text{UV})/Q_{\text{em}}(\text{IR})]^{1/4} > 1$
 - \rightarrow the resulting "**green-house effect**" pushes T_d **above** the Eddington value.
 - Fortunately, uncertainties in the correction term are muted by the 1/4 power.
- Let's use the Mie theory from above to estimate the correction term
 - First, consider the absorption efficiency for optical/UV starlight:
 - For grain sizes $\sim 0.1\mu\text{m}$, $X = 2\pi a/\lambda \approx 1 - 5$ for $\lambda \approx 5000\text{\AA} - 1000\text{\AA}$
 - $\rightarrow Q_{\text{abs}} \sim 1$ even for poorly absorbing grains ($m = 1.5 - 0.05i$) (see figure).
 - But, at longer wavelengths and smaller grains Q_{abs} drops well below 1
 - \rightarrow in practice, then, L_{\star} should be replaced by $L_{\star, \text{UV}}$ and Q_{abs} can be set to 1
- For $Q_{\text{em}}(\text{IR})$ we use Kirchoff's law and ask instead: what is $Q_{\text{abs}}(\text{IR})$?
 - Again, relying on Mie theory; for $\lambda \gg a$, we have $Q_{\text{abs}} \approx -4 \times \text{Im}[M]$
 - for $a \sim 0.1\mu\text{m}$, $X = 2\pi a/\lambda \sim 0.005$ in the FIR

$\text{Im}[M] \sim -0.5 \rightarrow -0.025$ for 1.5-1.0i (eg metal oxide) $\rightarrow m = 1.5-0.05i$ (eg an ice)
 $\rightarrow Q_{\text{em}}(\text{FIR}) = Q_{\text{abs}}(\text{FIR}) \sim 0.01 - 0.0005.$

- Thus, our correction factor to T_d is $(Q_{\text{abs}}/Q_{\text{em}})^{1/4} \sim 3 - 7$
 We expect ~ 3 for poor dielectrics/shorter wavelengths/warmer temps/larger grains
 We expect ~ 7 for good dielectrics/longer wavelengths/colder temps/smaller grains
- Using the modified equilibrium relation, we find:
 1. Interstellar dust, warmed by a weak isotropic radiation field: $J_s \sim 0.002 \text{ erg/s/cm}^2/\text{sr}$ yields

$$T_d \sim (\pi J_s / \sigma)^{1/4} \times (Q_{\text{abs}}/Q_{\text{em}})^{1/4} \approx 3.2 \times 5 \sim 15\text{K}$$
 This cold component is called interstellar "cirrus", and emits in the FIR $\sim 100\text{-}300\mu\text{m}$
 It is seen in other galaxies when not dominated by warmer (eg star formation) components
 It is slightly warmer in Ellipticals, with their higher interstellar radiation field.
 It probably shows a temperature gradient decreasing outwards, as J_s declines.
 2. Because they are complex environments, HII regions have a range of T_d
 Close to O stars $T_d \sim 50\text{K}$; In shrouded regions $T_d \sim 10\text{K}$
 Heating by trapped Ly α is often important: $T_d \sim 100\text{K}$
 3. Deep inside DMCs, shielded from all external radiation, $T_d \sim \text{few K}$
 Here, the source of heating is X-rays from the surrounding hot phase, and cosmic rays.
 4. In AGN the dust can be appreciably warmer, for example:
 using $L_{\text{AGN}} \sim 10^{10} L_{\odot}$ and grain green-house factor ~ 5 , we get
 \rightarrow Narrow Line Region ($\sim 100\text{pc}$) temperatures: $T_d \sim 100\text{K}$
 \rightarrow Broad Line Region ($\sim 0.1 \text{ pc}$) temperatures: $T_d \sim 3000\text{K}$
 AGN's typically have "warm" IRAS colors from NLR dust: $F_{25} / F_{60} \gtrsim 3 \times F_{60} / F_{100}$
 Note that dust may not survive in the BLR: $T_d \gtrsim T_{\text{sublimate}} \sim 2000 \text{ K}$ (check)

(iii) Thermal Spikes from Single Photons

- There are some puzzling observations:
 sometimes, where we expect $T_d \sim 30\text{K}$, we find 2 - $25\mu\text{m}$ emission $\rightarrow T_d \lesssim 1000\text{K} !!$
 there are galactic sources where T_d is **independent of distance** from the central star
 How do we understand these results?
- A population of **very small** grains: $\lesssim 100$ atoms; possibly PAH
 For these grains a **single UV photon** carries enough energy to heat the entire grain to $\sim 1000\text{K}$.
 e.g. 1000A photon has 10eV, and a grain of N atoms has thermal capacity $\sim 3Nk$ per Kelvin
 $\rightarrow 10\text{eV} = 3Nk\Delta T$ giving $\Delta T \sim 500\text{K}$ for an $N=100$ atom grain.
 \rightarrow well above the equilibrium temperature from a classical (non-photon) radiation field.
 Such hot grains radiate in the NIR
- However, they don't stay hot long !!
 At a few 100K they quickly radiate their thermal energy: $t_{\text{cool}} \lesssim 1 \text{ second}$
 These grains have a "spikey" thermal history: mostly cold, with brief spikes of a few 100K ([image](#))



(10) Dust: Emission & Absorption

- As expected, there are two types of emission/absorption associated with dust:

Continuum: thermal emission; and roughly λ^{-1} absorption and scattering
 Lines and Bands: both emission and absorption features.

- We have already encountered dust's thermal continuum emission;
 it is thought to be roughly Planckian, modified by an emissivity $\propto \lambda^{-1}$

Now let's look at the other emission and absorption signatures of dust.

(a) Line & Band Features

- Lines & band features derive from specific bond stretching or bending modes
 However, they are shifted and/or broadened due to the lattice environment.
 Most, though not all, of these features are now identified.
- Examples:
 - There is a very broad near-UV **absorption** feature centered at 2175Å
 it is thought to arise from a surface charge resonance on small (20nm) graphite grains.
 - The 3-12 μm region has several PAH features (**image**)
 e.g. 3.3, 6.2, 7.7, 8.6, 11.3, 12.7 μm
 these arise from various C-H and C-C bending and stretching modes.
 - Broad silicate absorption (and emission) features (see fig)
 - 3.1 μm : O-H stretch
 - 6 μm : H-O-H bend
 - 9.7 μm : Si-O stretch
 - 18 μm : Si-O-Si bend
 - The so-called Diffuse Infrared Bands (DIB) are emission/absorption features near ??-?? μm
 their total and relative strengths vary, though are relatively low
 their origin is still unknown. uncertain.

(b) Dust Absorption

(i) Basic Scenario

- Interstellar dust both **absorbs** and **scatters** light, blue more than red
 Stars therefore appear both fainter (extinction) and redder (reddening)
 The absorbed light is reradiated in the FIR & escapes the galaxy
 The scattered light contributes to the diffuse background light
 (and in certain circumstances can appear as a reflection nebula).
- Adopting a standard radiation transfer scenario (see fig)
 If $I_{0,\lambda}$ enters a region and I_λ emerges, with $I_\lambda(\text{abs})$ absorbed and $I_\lambda(\text{sca})$ scattered, then

$$I_\lambda = I_{0,\lambda} - I_\lambda(\text{abs}) - I_\lambda(\text{sca}) \quad \text{and} \quad I_\lambda / I_{0,\lambda} = \exp(-\tau_\lambda)$$
 where τ_λ is the extinction optical depth
- In terms of magnitudes of extinction, A_λ ,

$$A_\lambda = -2.5 \log_{10}(I_\lambda / I_{0,\lambda}) = -2.5 \log_{10}[\exp(-\tau_\lambda)] = 1.086 \times \tau_\lambda$$
 \rightarrow extinction in magnitudes **is**, roughly, the optical depth.
 Observationally, of course, A_λ gives an increase in apparent magnitude:
 e.g. for the V band: $A_V = m_V - m_{V,0} \equiv V - V_0$ (A_λ is always +ve)

(ii) Standard Extinction Law

- Extinction depends on wavelength, and many studies have tried to measure this dependence
 e.g. divide spectra of two stars of the same spectral type, only one of which is reddened. (figure)
 The results are surprisingly consistent, and one speaks of a **standard extinction law**
 (variations do exist (see below), and should be kept in mind as a source of uncertainty)

- One way to describe extinction is using the normalized function A_λ / A_V where $A_V = A_{\lambda=5500\text{\AA}}$
Here is a plot of A_λ / A_V : (figure)
It rises from zero in the IR, roughly as λ^{-1} , and peaks in the UV at 700\AA
There are features superposed at 2175\AA; 9.7 μm ; and 18 μm (see above)
(Note: because $A_\lambda \propto \lambda^{-1}$ over a wide range, extinction laws are usually plotted vs λ^{-1})
- A number of algebraic fits to this "reddening law" exist.
A commonly used one is given by Cardelli, Clayton, & Mathis (1989, ApJ 345 245) [e-link](#)
- A more physically based approach models the extinction curve using different dust populations
Two such models are shown here: [figures](#)
- The innocuous looking extinction curve hides an enormous variation in transparency:
For example: at 4400\AA $A_B/A_V \approx 1.33$ and at 5 μm $A_M/A_V \approx 0.023$
So, comparing extinction in the blue and mid-IR, we have $A_B / A_M \approx 57$
A good example is the Galactic center, for which:
→ $A_M \sim 0.6$ mag (57% transparent),
→ $A_B \sim 34.5$ mag ($1.6 \times 10^{-12}\%$ transparent -- utterly invisible) !!
- Note that since $A_\lambda \propto \lambda^{-1}$ at long wavelengths, we can obtain A_λ in the mid and far IR
e.g. $A_{60\mu} = 1/60 A_{1\mu} = 1/60 A_J$, and hence $A_{60\mu} = 1/60 \times A_J/A_V \times A_V = A_V / 212$.

(iii) Some Other Parameters

- So far, we have encountered A_λ and A_V , or in general A_X for band X (e.g. UBVRJHKLMN)
- Often, **reddening** is easier to measure than **extinction**
so another useful parameter is :
 $E_{B-V} = (B - V) - (B - V)_0 = A_B - A_V$ or its generic relative $E_{\lambda-V} = A_\lambda - A_V$
E values are differences in color and are therefore easier to measure
(you may know the color of an unreddened F5 star, but you don't know its apparent magnitude).
- Since all optical depths are additive, E_{B-V} and A_V are **proportional**
specifically, we define
 $R_V = A_V / E_{B-V} \approx 3.1$ for the standard extinction law.
Note that $1/R_V = (A_B - A_V) / A_V = A_B / A_V - 1$
which measures the **slope** of the extinction curve in the 4500\AA - 5500\AA region
Note that **bigger** values of R_V mean **shallower** slope and **less** UV extinction for a given A_V .
- Since E's are more easily measured than A's, the extinction law is often given in the form:
 $E_{\lambda-V} / E_{B-V}$ (see figure)
If R_V is known, one may obtain A_λ / A_V from the relation:
 $E_{\lambda-V} / E_{B-V} = R_V (A_\lambda / A_V - 1)$
Since extinction goes to zero as $\lambda \rightarrow \infty$, we have :
 $E_{\lambda-V} / E_{B-V} \equiv (A_\lambda - A_B) / (A_B - A_V) \rightarrow (-A_V) / (A_B - A_V) \equiv -R_V$
which is the usual way that R_V is measured.
Hence, if the **full** range of $E_{\lambda-V} / E_{B-V}$ is known, one may obtain A_λ / A_V

(iv) Variations in the Extinction Law

- Above $\lambda \sim 7000\text{\AA}$ (R), the extinction law seems quite universal
→ one can correct with confidence using the standard law.
this is because for $\lambda \gg a$, standard scattering theory works (see below), and $A_\lambda \propto \lambda^{-1}$

- Below $\lambda \sim 5500\text{\AA}$ (V), the form of A_λ can vary with both environment and metallicity (this is why B&M advocate A_J as normalization rather than A_V)
There has been considerable effort to characterize these variations.
- Generally, lower density and lower metallicity gives
→ weaker 2175Å feature and steeper UV slope (lower R_V)
Here's a comparison of three curves of decreasing metallicity: (figures)
MW → LMC → SMC : relative metallicities 1 → 1/2.5 → 1/7
- Similarly, there is some evidence for higher R_V (4-5) in DMCs
→ lower UV absorption, consistent with larger grains growing in the cold dense gas
- One version of the UV part of the extinction law makes these variations more explicit:
 $E_{\lambda-V} / E_{B-V} = [c1 + c2.x] + [c3.D(x)] + [c4.F(x)]$ for $x = \lambda^{-1} > 3.3\mu\text{m}^{-1}$ ($\lambda < 3000\text{\AA}$)
The three terms are roughly independent, and correspond to three grain populations:
 1. $[c1 + c2.x]$: large "classical" grains. Slope (c2) depends on size distribution:
slope decreases as $\langle a \rangle$ increases (higher R_V).
 2. $[c3.D(x)]$: small (20nm) graphite grains.
 $D(x)$ sets the location & width of the 2175Å feature.
 3. $[c4.F(x)]$: v. small (dielectric?) grains which affect the FUV (1100-1700Å) part
 $F(x)$ is cubic polynomial fit to FUV rise after linear and 2175Å features removed.
- Finally: knowledge of the extinction law in other galaxies (besides LMC,SMC) is still rudimentary.
Hopefully, the various grain populations identified locally are nevertheless present.

(v) Correcting for Reddening and Extinction

- Often, dust is simply a nuisance, and we need to correct for the effects of extinction:
This involves three steps:
 1. choose an extinction law (usually, the standard one)
 2. estimate A_V using something of known color
 3. apply the corrections, both to color and, if needed, flux.
- Here's an approach suited to an emission line spectrum:
consider two emission lines at λ_1 and λ_2 with **true** fluxes F_1 and F_2
Their **observed** fluxes are:
 $f_1 = F_1 \text{ dex}(-0.4 A_{\lambda_1})$ and
 $f_2 = F_2 \text{ dex}(-0.4 A_{\lambda_2})$
writing observed and true flux ratios as $f_1/f_2 = r_{1,2}$ and $F_1/F_2 = R_{1,2}$,
and noting that $A_{\lambda_1} = A_V \times (A_{\lambda_1}/A_V)$, and $A_{\lambda_2} = A_V \times (A_{\lambda_2}/A_V)$, we have
 $r_{1,2} = R_{1,2} \text{ dex}[-0.4 (A_{\lambda_1} - A_{\lambda_2})]$
giving
 $-2.5 \log_{10} (r_{1,2}/R_{1,2}) = A_V [(A_{\lambda_1}/A_V) - (A_{\lambda_2}/A_V)]$
Hence, from measured $r_{1,2}$, and knowing $R_{1,2}$ and the extinction law A_λ/A_V , we can derive A_V
- Once A_V is known, it is straightforward to correct any other flux or flux ratio.
for example :
 $F_3 = f_3 \text{ dex}[+0.4 A_V \times (A_{\lambda_3}/A_V)]$, and
 $R_{3,4} = r_{3,4} \text{ dex} [+0.4 A_V \times [(A_{\lambda_3}/A_V) - (A_{\lambda_4}/A_V)]]$
- We need some initial line ratios where we **know** their unreddened values.
There are several to choose from, but usually the **Balmer series** is used.
For a wide range of conditions, the Balmer series have case B ratios:

$$\boxed{\text{H}\alpha \text{ (6563\AA)}} \quad \boxed{\text{H}\beta \text{ (4861\AA)}} \quad \boxed{\text{H}\gamma \text{ (4340\AA)}} \quad \boxed{\text{H}\delta \text{ (4101\AA)}}$$

2.86	1.00	0.47	0.26
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So, for example, for a **measured** $H\alpha/H\beta$ ratio, we derive A_V from :

$$A_V = -2.5 / [A_{H\alpha} - A_{H\beta}] \times \log_{10} [(H\alpha/H\beta) / 2.86]$$

where $A_{H\alpha}$ is A_{6563A}/A_V is given by the extinction law (similary for $A_{H\beta}$)

For the standard extinction law, we get

$$A_V = ?? \times \log_{10} [(H\alpha/H\beta) / 2.86]$$

- Be careful in your choice of Hydrogen recombination lines.
The Lyman and Balmer/Lyman ratios often suffer optical depth effects and deviate from case B. This is especially true at high densities, e.g. in AGN BLRs and even AGN NLRs. Usually, however, Balmer, Paschen, and Brackett series are OK
The exception is $H\alpha/H\beta$ which in AGN NLRs is closer to 3.1 than 2.86.
- This whole analysis assumes the source lies behind a **uniform screen** of dust
Be careful: if the emission region is itself pervaded by dust things are more complicated
each color samples a different volume (more in the red)
the dust may itself alter the ionization/emission structure of the region.
the gas phase abundances may also be altered by depletion onto dust.
Usually, there is insufficient information to improve on the foreground screen analysis.

(vi) Dust to Gas Ratios

- To first order, extinction & reddening are proportional to **total hydrogen column** (figure)

$$E_{B-V} \approx 1.72 \times 10^{-22} N_H \text{ mag}$$

$$A_V \approx 5.34 \times 10^{-22} N_H \text{ mag}$$

where N_H (in cm^{-2}) is summed over H^+ , HI, and H_2

the quantity E_{B-V}/N_H is called the **dust to gas ratio**

- A **physical** measure of dust to gas ratio is
 $Z_d = (\text{mass in dust})/(\text{mass in H + He})$
for solar metallicity, complete depletion yields $Z_{d,\odot} = 0.016$
- there is some evidence that the D-to-G ratio is **lower** (less dust) in
hotter ISM phases
higher velocity clouds
consistent with dust destruction in shocks.
- Not surprisingly, a lower metallicity also seems to lower the total gas/dust ratio
 $A_V = 17 \times 10^{-23} R_V N_H$ (MW)
 $A_V = 4 \times 10^{-23} R_V N_H$ (LMC)
 $A_V = \sim 3 \times 10^{-23} R_V N_H$ (SMC)

(vii) X-ray Absorption

(viii) Polarization



(11) Dust Emission from Galaxies

- The appearance of dust in galaxies has a long History: (see [Topic 1.2c](#))
In 1920 Curtis used dust lanes to argue (correctly) for the external nature of Spiral Nebulae, edge on nebulae have dark lanes which resemble the Milky Way's "zone of avoidance"
→ Spiral Nebulae are **external** versions of MW.
- Dust is **ubiquitous**: it is found in ~all galaxies; and throughout each galaxy (e.g. [Sombrero](#)) however, its role can vary greatly from one galaxy to the next.
- The subject has developed **slowly**: recent progress has been due mainly to advances in **IR detection**.

(a) Absorption of Galaxy Light

- since dust size $\approx 0.5\mu\text{m}$ it absorbs UV & optical efficiently
This can have two important impacts on our measurement of galaxies:
it affects the optical/UV **appearance**, hiding important regions
it can significantly reduce their **apparent luminosity**,
→ undermines studies of, e.g., M/L ratios; Tully-Fisher relation; Dark Matter.
Need to understand and correct for this absorption.
One approach: study how galaxy photometry depends on **galaxy inclination**.

(i) Inclination Effects

- This also has a long history; Holmberg (1950s) plots $\langle\mu_B\rangle$ vs a/b (mean surface brightness vs inclination)
On average, as galaxies change from face on to edge on, one expects:
if optically **thin**, one expects inclined galaxies to be **brighter** (same light, less projected area)
if optically **thick**, one expects inclined galaxies to be **same or dimmer** (only see to $A_V \sim 1$).
→ he finds dust dimming is **modest-to-important**
- Since then, there have been many "correction formulae" published: $\delta m_i = f(a/b, \text{Hubble Type})$ [[Topic 3.7e](#)]
Applying these corrections **reduces scatter** in astrophysically meaningful plots (figure)
- Be alert: some formulae correct to "face on"; others to "dust free", e.g.
RC3 corrects to face on
RSA corrects to dust free
these can differ in B by ~ 1 mag for the same galaxy !

(ii) Perpendicular Opacity of Disks

A critical question is whether disks are optically thick or thin.... Much debate in the 1990s. Without rehashing that debate, it now seems that disks are:

optically thick towards the center, but transparent at the edges
thick in patches, particularly near spiral arms
there can be significant variations between galaxies.

In response to the overall uncertainties,

→ most work on M/L ratios (e.g. TF relation) is now done **in the near IR** (I or H band)

(iii) Hidden Star Formation

Near-IR & Mid-IR imaging can reveal optically invisible star formation regions

- in normal spiral disks, obscured SF knots can be seen in spiral arms (e.g. M51)
- in starbursts, much dust is made which obscures the optical light.
→ buried super star clusters emerge in the IR (e.g. [the antennae](#))
→ from SB to LIG to ULIG; L_{FIR} up by 10^3 while L_{opt} up by only $\times 3$ (see [Topic 11.7d](#) and [SED image](#))
- At the highest luminosity, there is a population of optically invisible $z \sim 2$ ULIGs

→ probably young, buried SB/QSO before blow-out.

(b) Emission: Broad Band SEDs

- FIR emission from dust is a ubiquitous feature of galaxy spectra since stars emit **no** radiation beyond 25μ , dust **dominates the Mid- Far-IR**
Since starbursts & AGN are powerful UV emitters, & dust is a good UV absorber:
→ sometimes, Mid-Far-IR from dust dominates **entire** galaxy SED
- As an example, here is the MW's ISM SED, and the SED of two AGN: **figures**

(i) Four Contributions to the FIR

Mid- and Far-IR emission can have varying contributions from :

1. Cold dust in the general ISM heated by the blue/UV ISRF ("cirrus")
 $10 - 30\text{K} \rightarrow 60 - 500\mu$
2. Warmer dust in molecular clouds heated by nearby star formation
 $50 - 100\text{K} \rightarrow 25 - 100\mu$
3. Yet warmer dust heated by an AGN
 $150 - 200\text{K} \rightarrow$ adds a 25μ component
4. Hotter dust in winds from evolved red giants
 $100 - 1000\text{K} \rightarrow 12 - 25\mu$

(ii) Other Factors Affecting the IR output

- a. Current & past star formation rates
UV output is a strong function of age (highest for **current** massive star formation).
- b. Metallicity & dust composition/size distribution
composition & particle size affects absorption & radiation (e.g. single photon heating)
- c. Relative location of dust & sources of radiation
UV **flux** defines eqm dust temperature (dust **close** to SF; galaxy nuclei; is warmer)

(iii) Variation Along the Hubble Sequence

- A number of properties vary systematically along the Hubble sequence, E → Sc (see **Topic 2.9**)
e.g. star formation rates increase & HI content increases
→ one might expect **systematic variation** of FIR/dust emission with Hubble sequence.
- Often **color-color** plots are useful
e.g. for IRAS with 4 bands: 12μ 25μ 60μ 100μ , one can define colors in **two** common ways:
 1. Log of flux ratio $[12]/[25] \equiv \log(F_{12}/F_{25})$, with $F_{12} = f_\nu$ at 12μ in Jansky's (i.e. per Hz)
 2. An effective two-point spectral index, e.g. α_{12}^{25} , where α is defined by $f_\nu \propto \nu^\alpha$

Here are two such plots for various galaxy types: (image)

- Understanding these FIR color-color plots was slow to develop
One must consider **two** dust types:
 - a. large grains at eqm temp, which increases with SFR
these affect the $25\text{-}60\text{-}100\mu$ fluxes
 - b. small stochastically (quantum) heated grains with \sim fixed (high) temperature
these affect the $12\text{-}25\mu$ fluxes
 And **three** radiation fields:
 - a. high flux UV field from young stars
 - b. UV from older population, whose flux depends on stellar density
 - c. an AGN, if present.

- The FIR colors arise in the following way:
 - Low SFR disks (e.g. Sa) have cirrus so cold that its 25μ flux is very low:
 - the large grains have **low** (cold) $[60]/[100]$
 - the small grains have \sim equal F_{12} & F_{25}
 - high SFR in irregulars (Sdm - Im) have warmer large grain emission,
 - $[60]/[100]$ is **higher**, and begins to dominate the F_{25} band
 - with F_{25} rising fast, the $[12]/[25]$ now appears **low**
 - In ellipticals & SOs, there is little/no star formation, however:
 - Es & SOs have high stellar densities in the bulge with correspondingly high ISRF dust, if it is present, is usually in the **nuclear** regions, where the ISRF is high.
 - cirrus has intermediate temperature, with intermediate $[12]/[25]$ & $[60]/[100]$
 - FIR luminosities consistent with heating by UV from post AGB stars ($r \lesssim 1$ kpc) (there is still some disagreement over whether red giant winds contribute in E/SOs).
 - Dust composition is also relevant:
 - It seems: from Im (low Z) → E (high Z), small/large grain ratio increases.

(iv) Starbursts

The IR SEDs of starbursts is discussed in [Topic 11.7d](#)
Briefly, as the luminosity of the starburst increases (see [image](#))

- L_{IR} increases correspondingly; $\sim \times 10^3$ @ ULIGS
- however, absorption suppresses **optical** increase to $\sim \times 3-4$
- dust temperature gets **warmer**, mainly at 60μ (30-60K)

(v) AGN

- Accretion power in AGN generates an intense "hard" spectrum
This can heat dust in the near-nuclear regions.
 - in the kpc-scale NLR, $T_d \sim 150-200K$ giving a 25μ component.
 - in the sub-pc scale BLR, $T_d \sim 500-1000K$
can give a Near-IR component $1-5\mu$ (though may not survive)
- At higher luminosity, the dust signature may depend on age:
 - early: post-merger, SB+AGN, shrouded
 - late: ISM blown away, SB declines → bare AGN dominated SED.

(c) Emission: Spectral Features

While the IR has many spectral features, there are two major features attributable to dust:

1.

